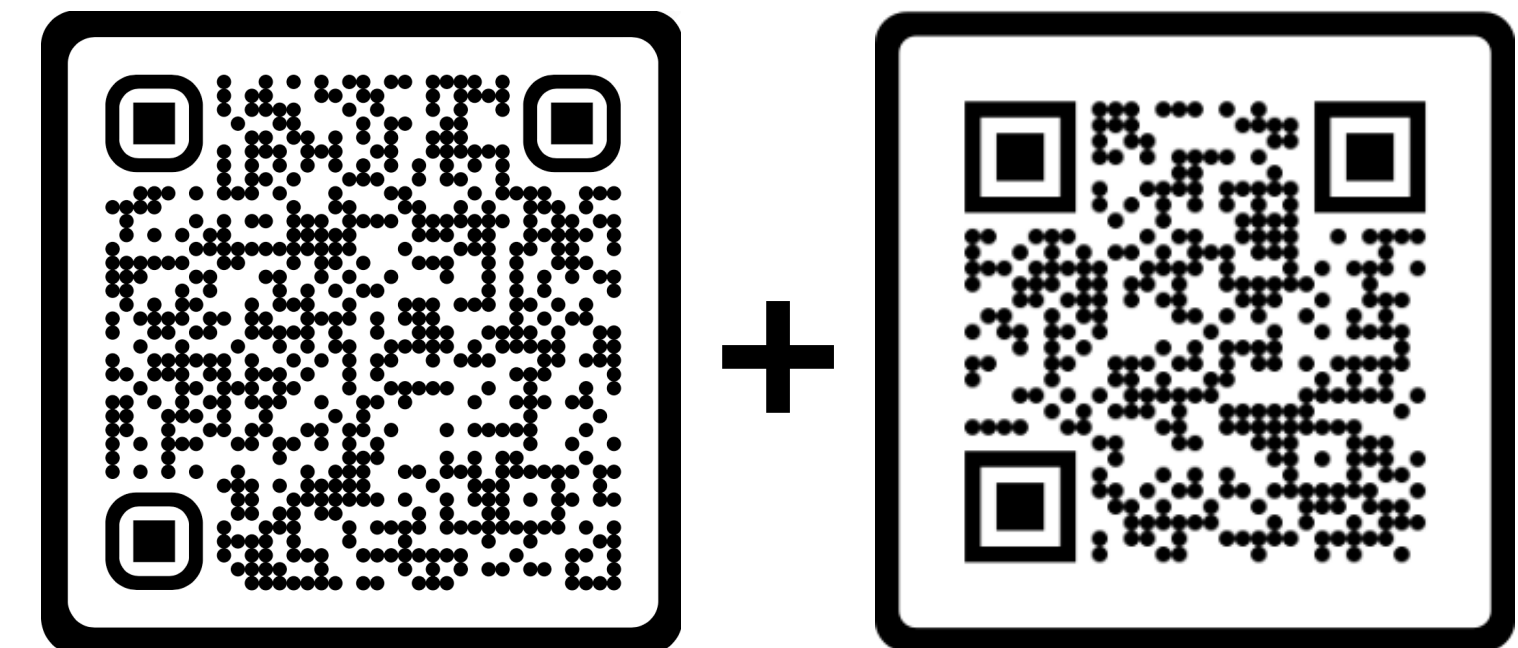


# Disaggregated Interventions to Reduce Inequality + Counterfactuals for the Future

DSGA-1017 Responsible Data Science  
Spring 2023

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# Outline

1. Disaggregated interventions to reduce inequality
  - Problem definition
  - Causal inference and social categories
  - A causal framework for addressing pre-existing inequalities
2. Counterfactuals for the future
  - Motivating example
  - Forward-looking counterfactuals
  - Empirical exploration

# Disaggregated Interventions to Reduce Inequality

# Three types of algorithmic bias

[Friedman, Nissenbaum 1996], [Stoyanovich, Howe, Jagadish 2020]

- **Pre-existing bias**
  - Originates in society and exists independently of an algorithm
- **Technical bias**
  - Introduced or exacerbated by the technical properties of an algorithm
- **Emergent bias**
  - Arises in the context of an algorithm's use

# Three types of algorithmic bias

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# Problem definition

# The “impact remediation problem”

## Formalizing pre-existing bias

1. We observe an existing disparity. We consider it undesired.
2. We have the ability to perform an intervention.
3. We want to decrease the measured disparity.

### Example:

1. Gender imbalance in a job applicant pool
2. Hosting booths at different career fairs
3. Rebalance our applicant pool

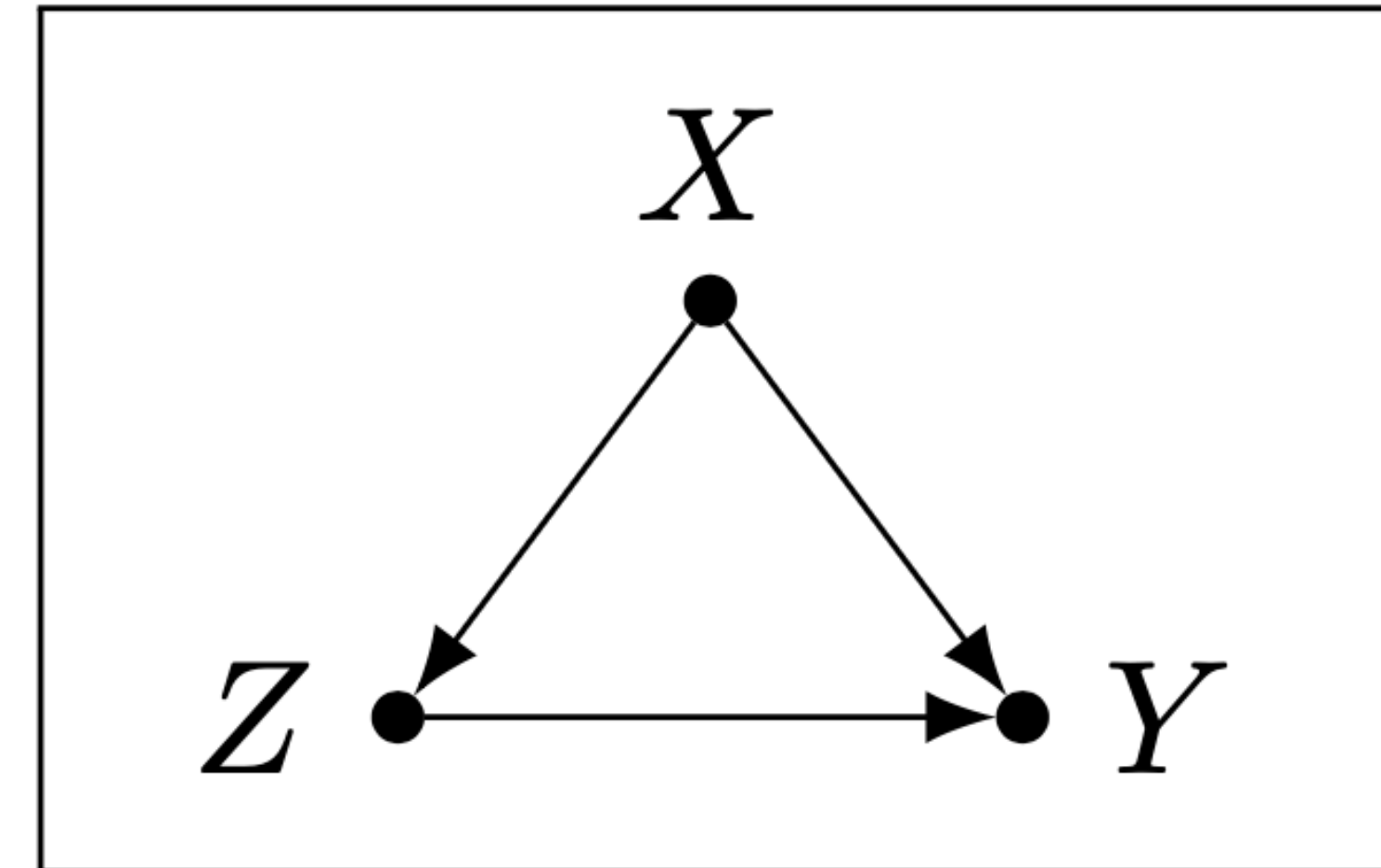
# Causal inference and social categories



# Structural causal models (SCMs)

[Pearl 2009], [Peters et al. 2017]

- An SCM is a four-tuple  $(U, V, F, P_U)$ 
  - $U$ : a set of exogenous background variables
  - $V$ : a set of endogenous observed variables
  - $F$ : a set of functions (structural equations) for each  $V_i \in V$
  - $P_U$ : a distribution over the exogenous variables  $U$
- Each SCM entails a directed acyclic graph (DAG)



$$X = \epsilon_X$$

$$Z = -1 + X + \epsilon_Z$$

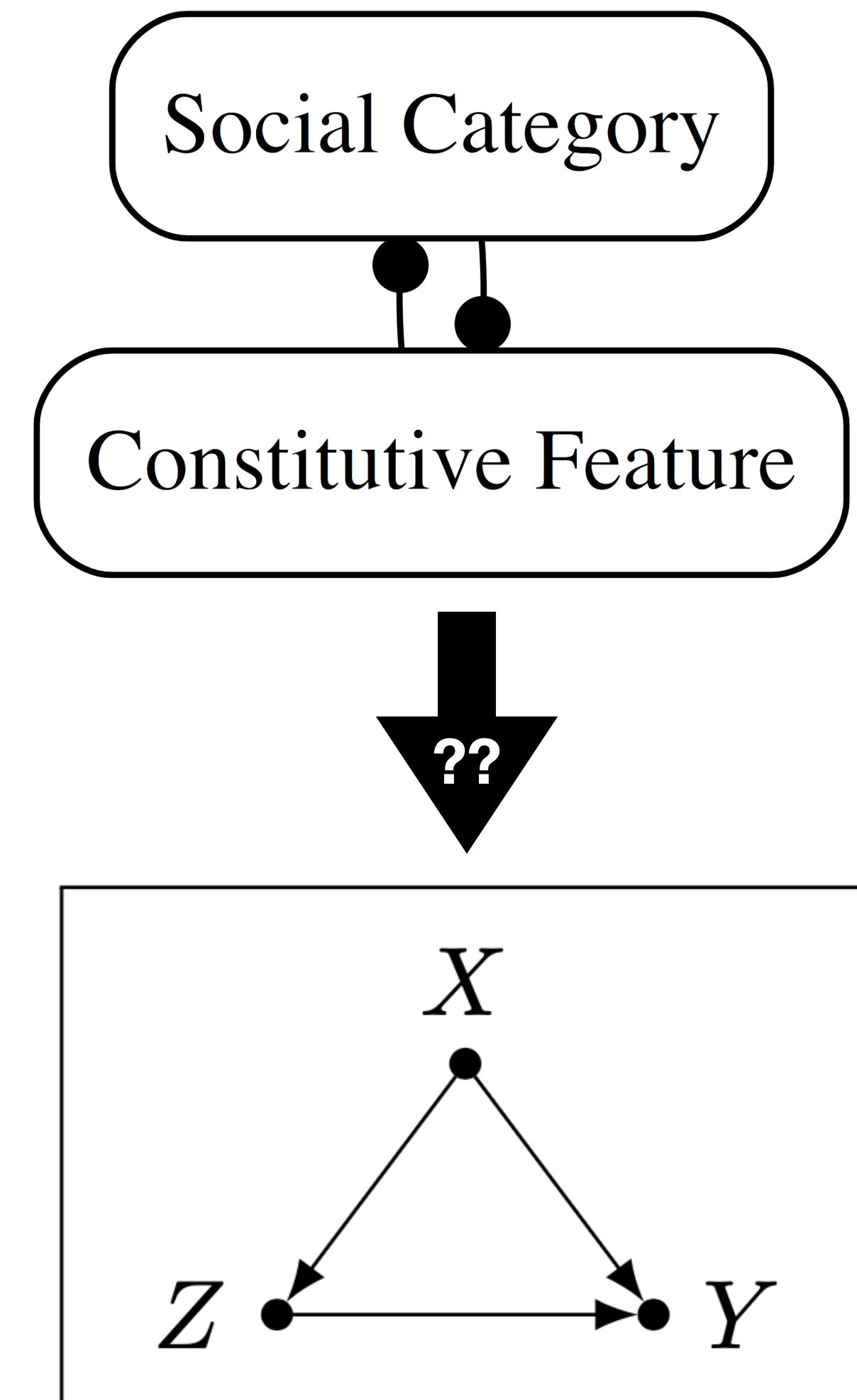
$$Y = 2 \cdot Z + X + \epsilon_Y$$

$$\epsilon_X, \epsilon_Y, \epsilon_Z \sim \mathcal{N}(0,1)$$

# Social categories and constitutive features

[Benthall and Haynes 2019], [Hanna et al. 2020], [Sen and Wasow 2016], [Hu and Kohler-Hausmann 2020], [Jacobs and Wallach 2021], [Kasirzadeh and Smart 2021]

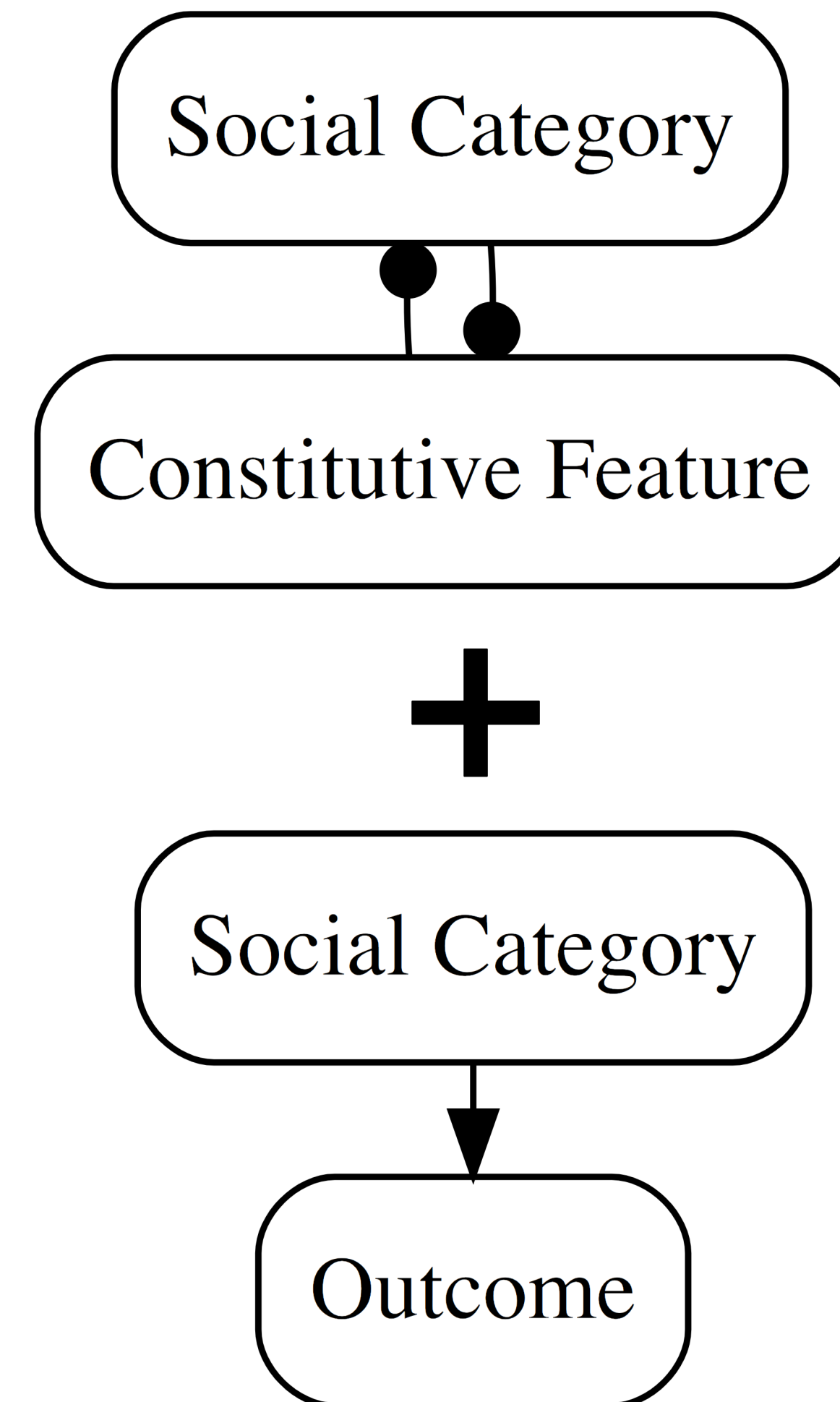
- Inequality involves social categories (e.g. race, gender)
- Two types of features:
  - **Regular feature:** causal, diachronic
    - Unfolding over time via cause-and-effect
    - “If A then B then C...”
  - **Constitutive feature:** a feature that defines a social category
    - Synchronous, definitional [Hu and Kohler-Hausmann 2020]
    - “If A then the definition of B has changed...”
- How to write down a DAG? → instantaneous constitutive **cycle**
- Examples:
  - Intuition: water + number of hydrogen atoms
  - Racial categorization + socioeconomic history
  - Simple variables (e.g., race + net worth), complex constructs



# Interventions on social categories

[Benthall and Haynes 2019], [Hanna et al. 2020], [Sen and Wasow 2016], [Hu and Kohler-Hausmann 2020], [Jacobs and Wallach 2021], [Kasirzadeh and Smart 2021]

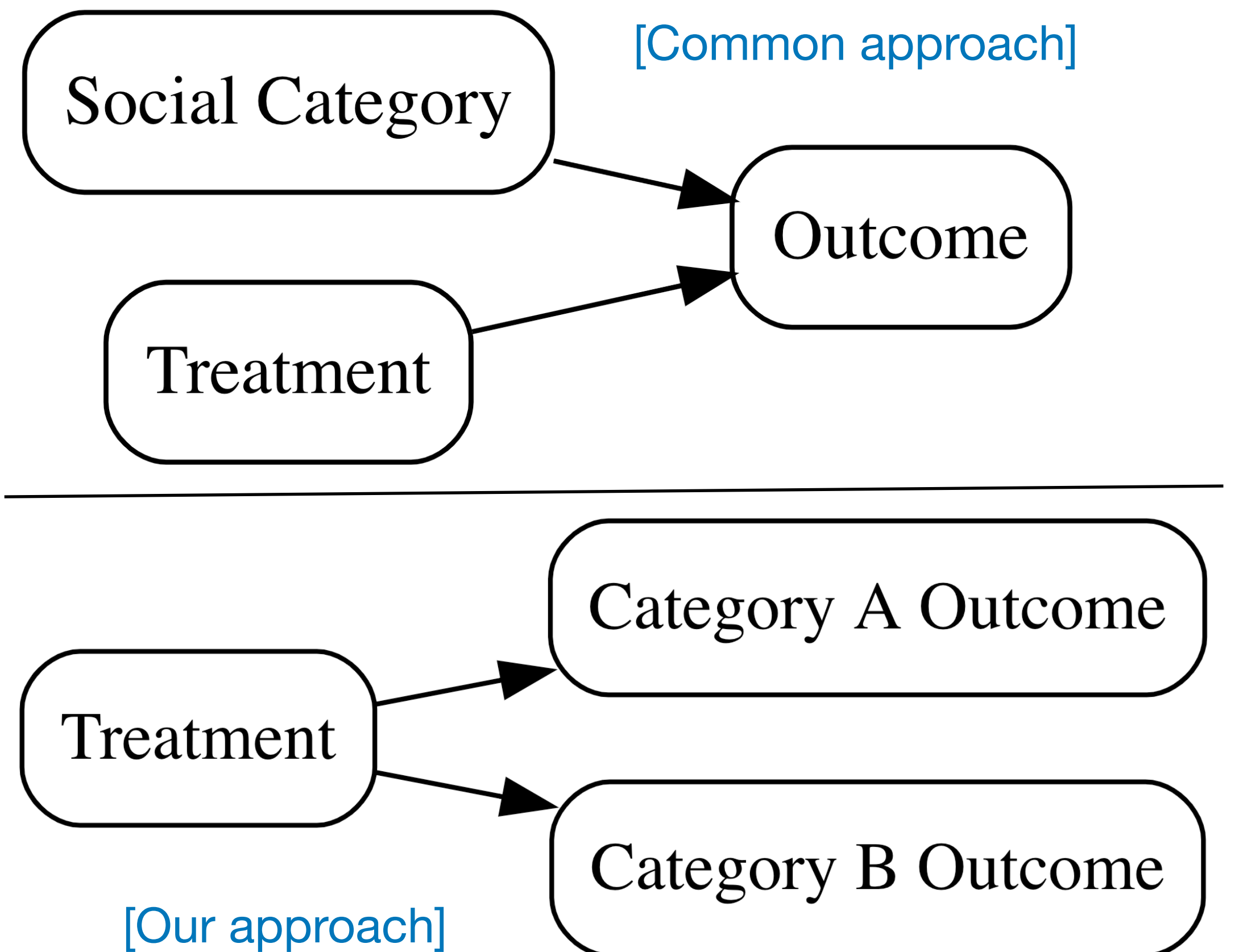
- Questions for interventions on race:
  - Are manipulations defined?
  - Post-treatment bias
  - Is the social category well-defined? Stable?
- **Simplified positions:**
  1. Defining counterfactuals via exposure to a racial cue  
  
vs.
  2. Not using causal models with race at all
- **Unavoidable problem:** racial disparities still exist (and other social category disparities)



# Social categories in impact remediation

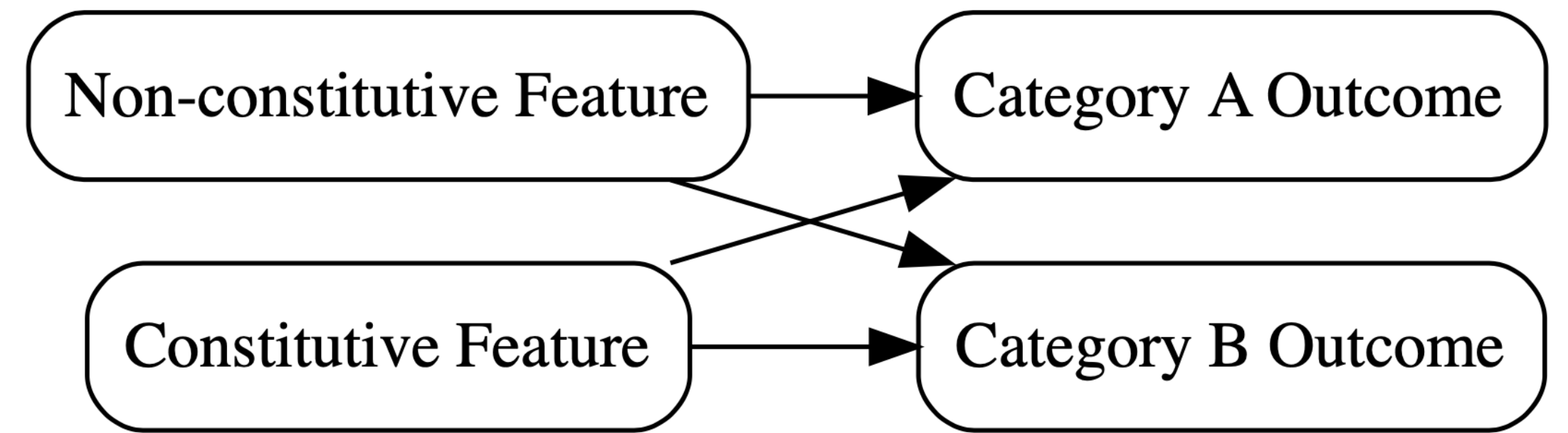
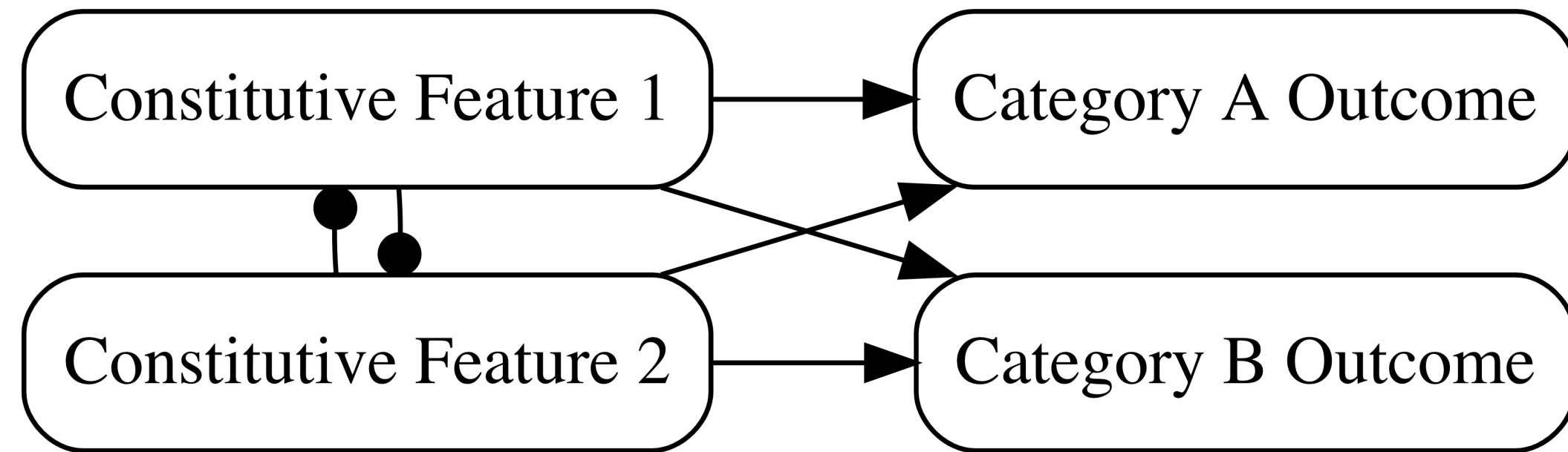
## Disaggregation to the rescue!

- **Approach:** *measure* a disparity across groups of people
  - Racial categories, genders, disabilities
- Our required assumption about social categories:
  - “A social category consists of a group of people” — no shared attributes necessary
- **Takeaway:** we don’t need to resolve the philosophical debate to tackle pre-existing disparities



# Social categories in impact remediation

Nuance: one constitutive feature at a time



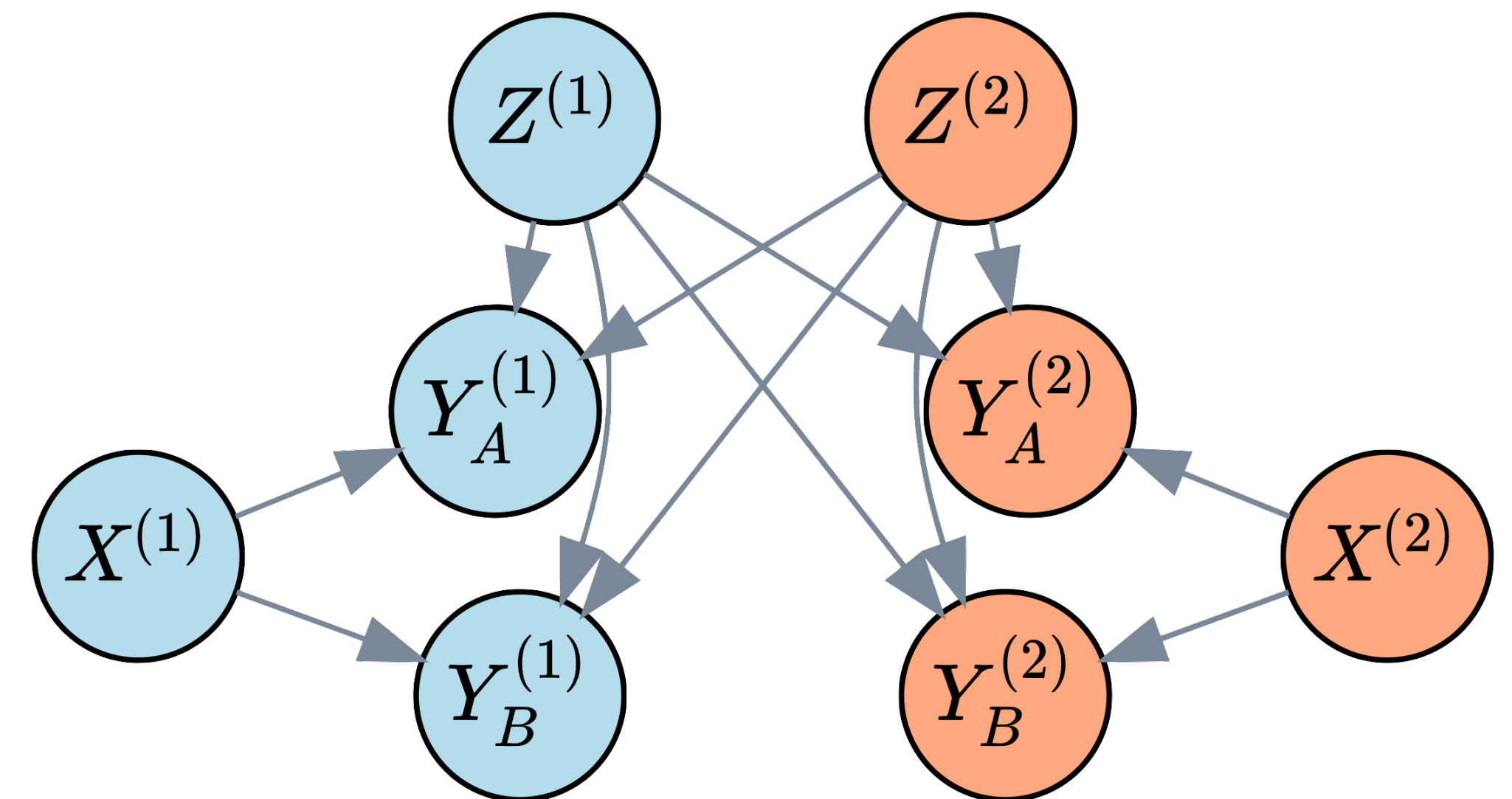
# Framework formalization

# Impact remediation – toy example

## A multi-level, nested intervention structure

Framework	Example
n individuals	425 potential job applicants
m sub-populations on which we can intervene (“intervention sets”)	2 universities
r sub-populations across which we see disparity	Female (A) and Male (B) gender groups
outcome of interest Y, disaggregated across r groups	Y = fraction of students who applied for the job
real-world features X	X = number of career counselors
possible intervention Z	Z = whether or not we hosted a booth at the career fair

Causal graph relating X, Y, Z



extension of [Kusner et al. 2019] + disaggregation

# Finding optimal interventions to decrease disparity

## Example: outreach in a job applicant pool

- Students in each gender group:

$$n_A^{(1)} = 100, \quad n_A^{(2)} = 75, \quad n_B^{(1)} = 150, \quad n_B^{(2)} = 100$$

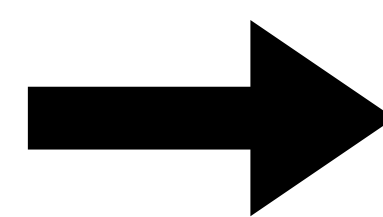
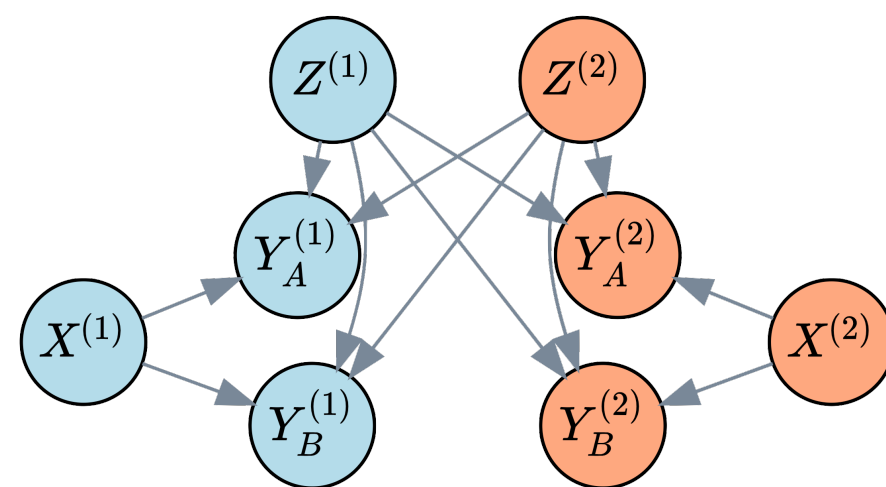
- Observed application rates:

$$(Y_A^{(1)}, Y_B^{(1)}) = (0.10, 0.20) \qquad (Y_A^{(2)}, Y_B^{(2)}) = (0.05, 0.10)$$

- Measure of disparity:

$$\delta(z) = \left| \frac{1}{n_A} \sum_{i=1}^2 n_A^{(i)} \mathbb{E}[Y_A^{(i)}(z)] - \frac{1}{n_B} \sum_{i=1}^2 n_B^{(i)} \mathbb{E}[Y_B^{(i)}(z)] \right|$$

- Estimated application rates *after* intervention:



$$\mathbb{E}[Y_A^{(1)}([z^{(1)} = 1, z^{(2)} = 0])] = 0.20$$

$$\mathbb{E}[Y_A^{(2)}([z^{(1)} = 1, z^{(2)} = 0])] = 0.10$$

$$\mathbb{E}[Y_B^{(1)}([z^{(1)} = 1, z^{(2)} = 0])] = 0.30$$

$$\mathbb{E}[Y_B^{(2)}([z^{(1)} = 1, z^{(2)} = 0])] = 0.15$$

$$\mathbb{E}[Y_A^{(1)}([z^{(1)} = 0, z^{(2)} = 1])] = 0.15$$

$$\mathbb{E}[Y_A^{(2)}([z^{(1)} = 0, z^{(2)} = 1])] = 0.15$$

$$\mathbb{E}[Y_B^{(1)}([z^{(1)} = 0, z^{(2)} = 1])] = 0.25$$

$$\mathbb{E}[Y_B^{(2)}([z^{(1)} = 0, z^{(2)} = 1])] = 0.15$$

- Disparity after intervention:

$$\delta \approx 0.08$$

no intervention

$$\delta([z^{(1)} = 1, z^{(2)} = 0]) \approx 0.08$$

university one

$$\delta([z^{(1)} = 0, z^{(2)} = 1]) = 0.06$$

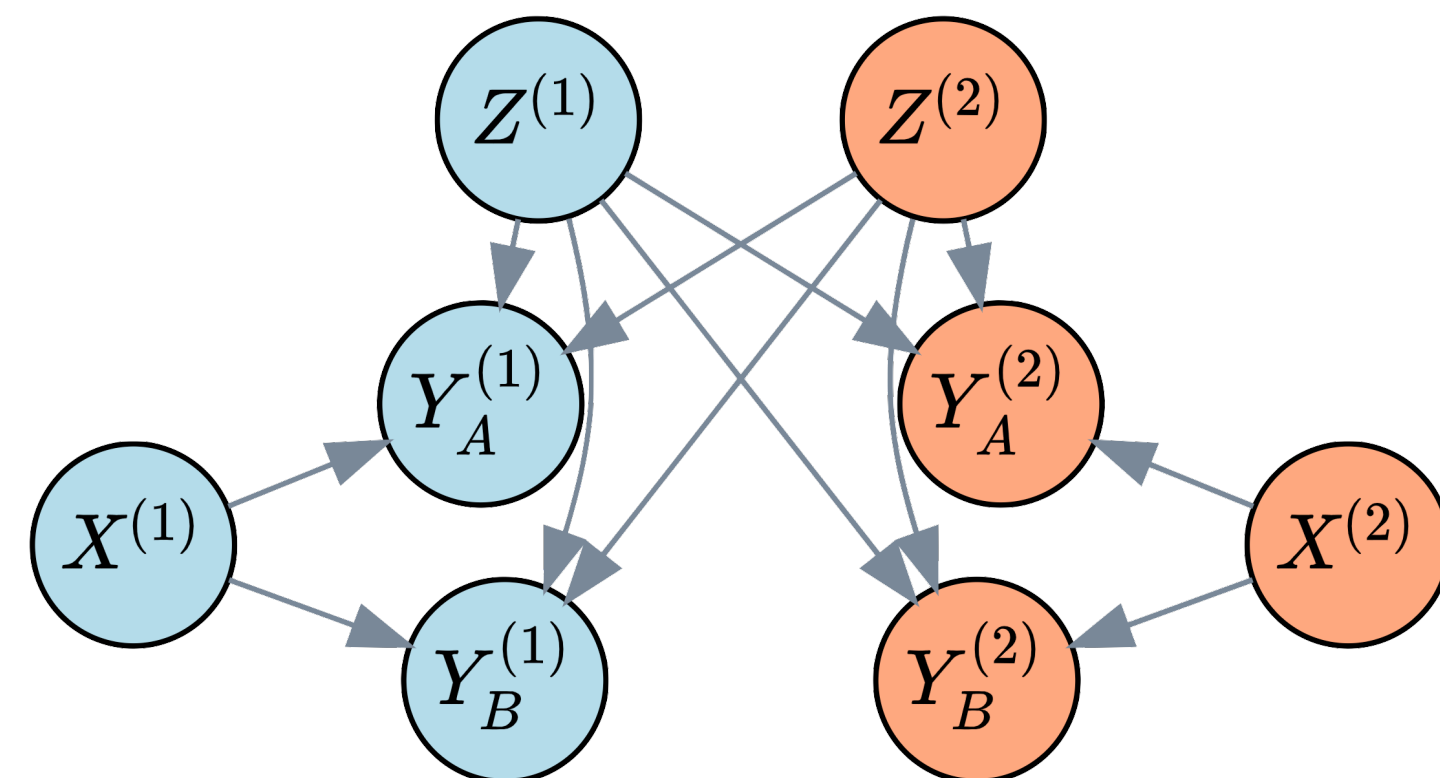
university two



# Impact remediation (IR) overview

Process overview:

1. Social categorization + data collection
2. Fit causal model to estimate intervention effects
3. Define our objective (how to mitigate disparity)
4. Find optimal interventions subject to constraints (budget, etc.)



$$\min_{z \in \{0,1\}^m}$$

s.t.

$$\left| \frac{1}{n_A} \sum_{i=1}^2 n_A^{(i)} \mathbb{E}[Y_A^{(i)}(\mathbf{z})] - \frac{1}{n_B} \sum_{i=1}^2 n_B^{(i)} \mathbb{E}[Y_B^{(i)}(\mathbf{z})] \right|$$
$$\sum_{i=1}^m z^{(i)} \leq b$$

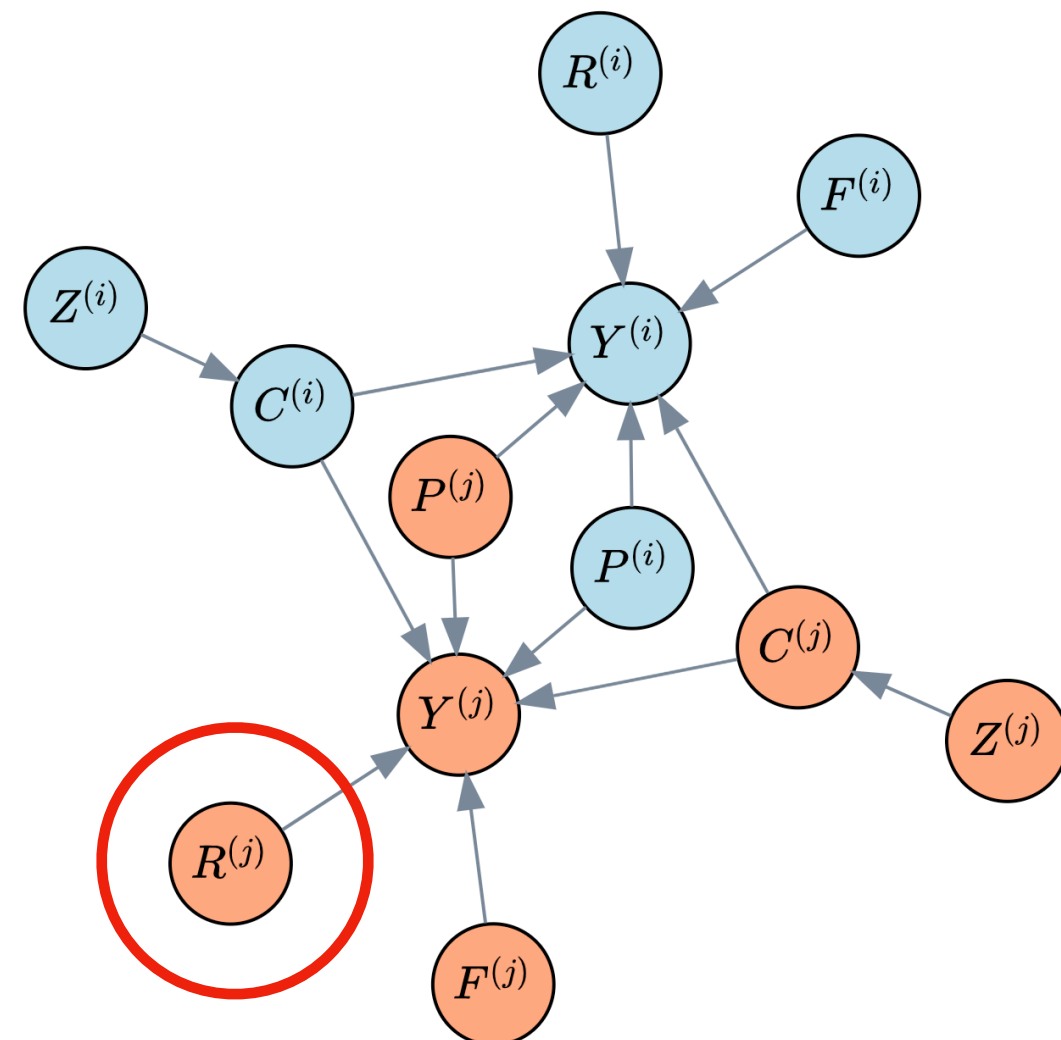
# Case study

# Stylized NYC schools example

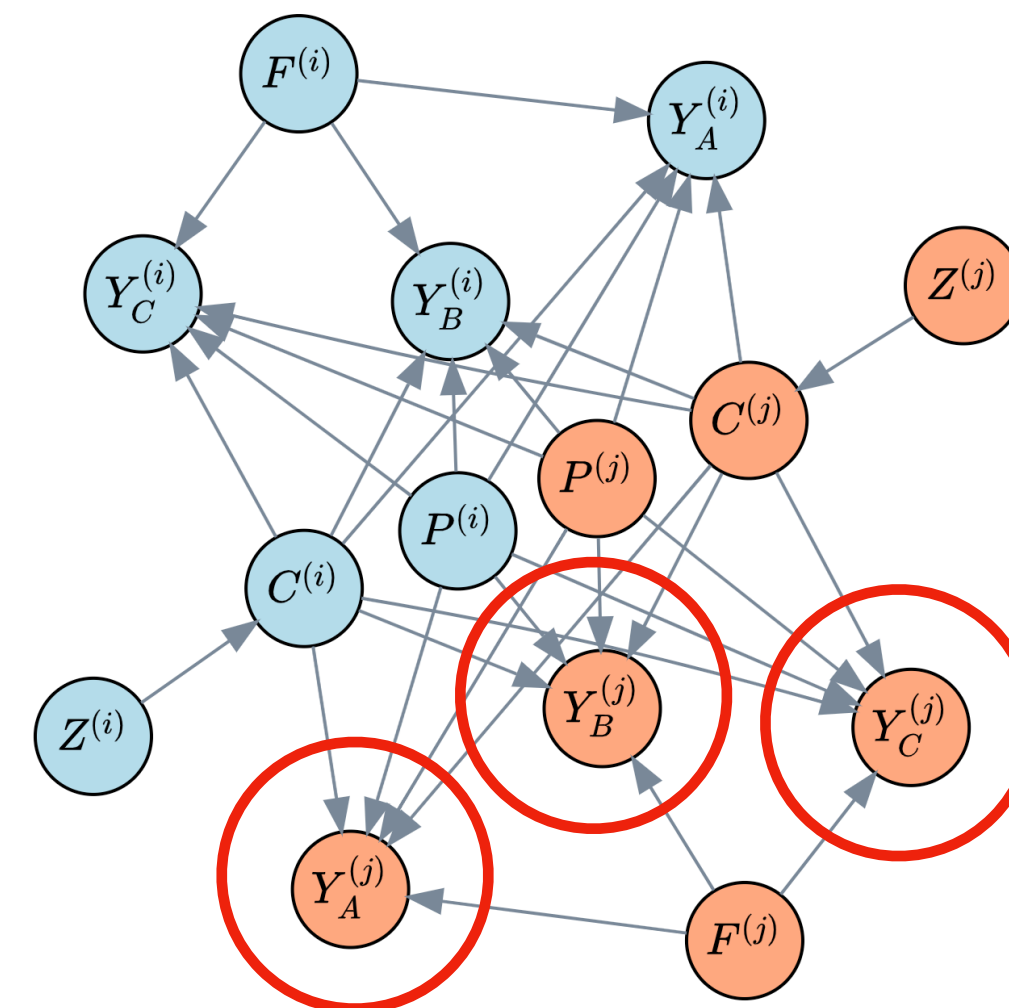
## An IR case-study

- An example with realistic data:
  - **Setup:** The US DOE giving funding to NYC public schools to hire Calculus teachers
  - **Goal:** increase college attendance
  - **Subgroups:** racial and gender categories

Causal Fairness  
[Kusner et al. 2019]



vs.

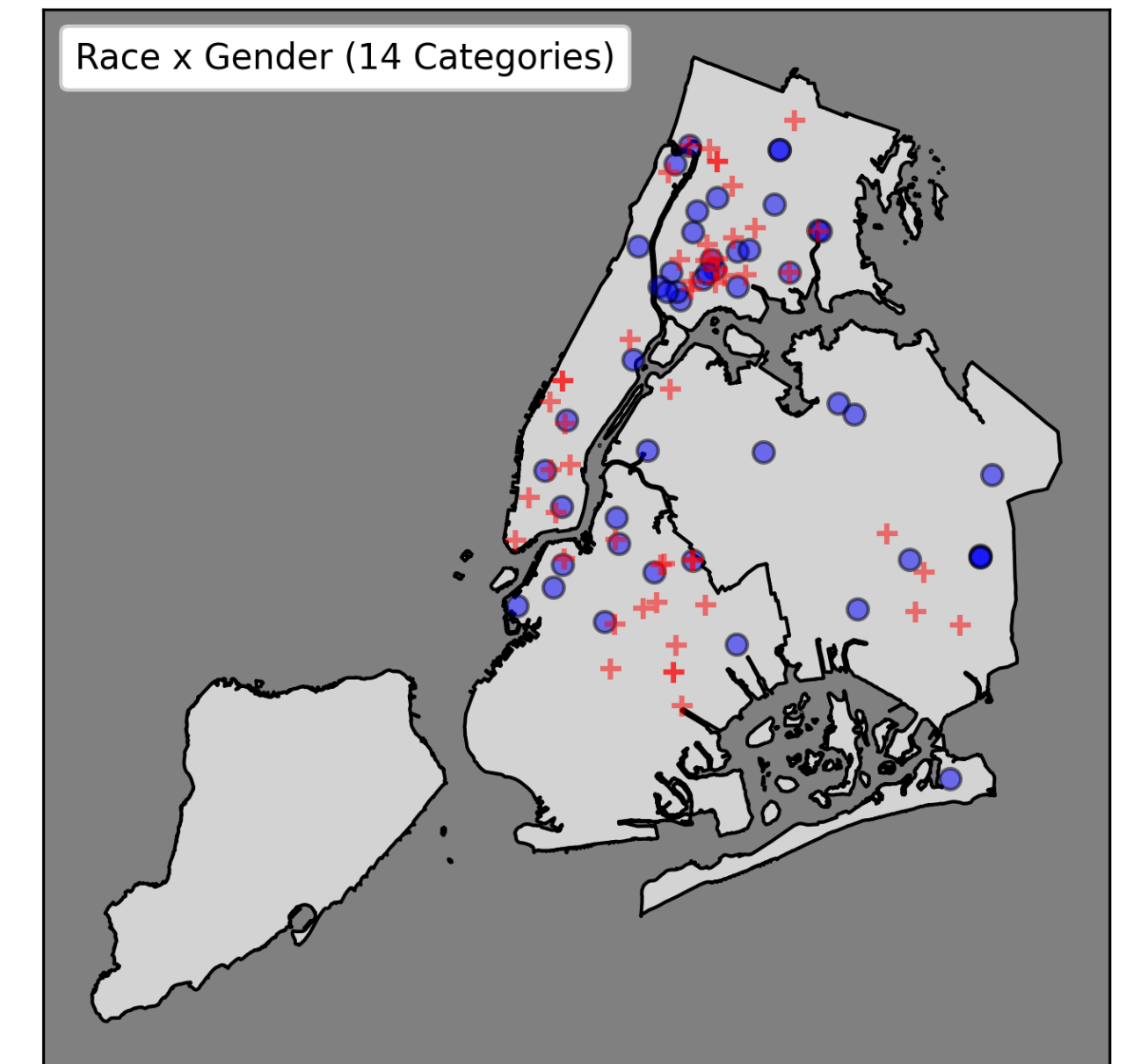
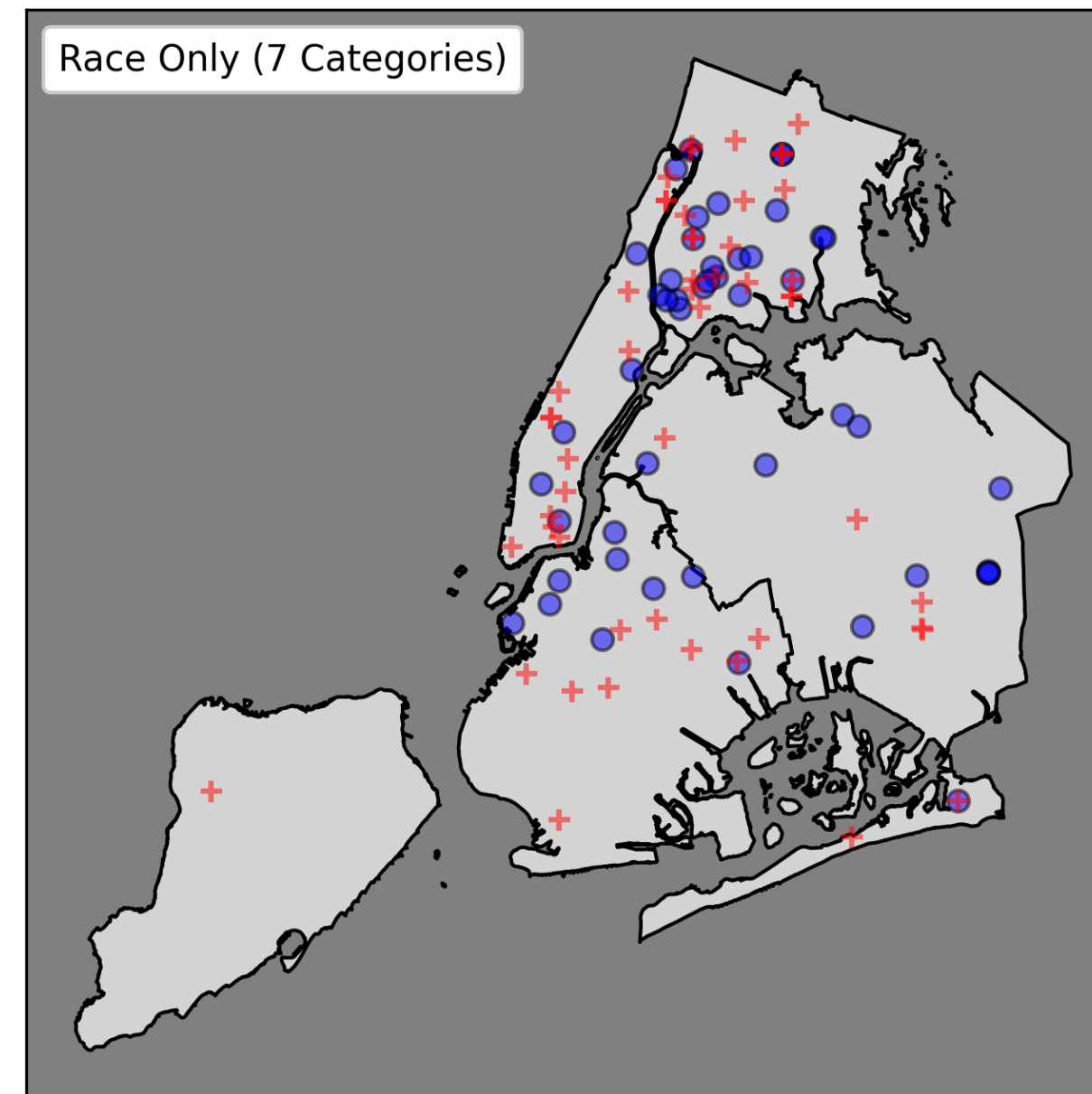


Focus on Inequality  
(disaggregation)

# Stylized NYC schools example

## Takeaways from a case-study

- Social categorization (i.e., which partition) changes results
- Measuring subgroup outcomes better allows for focus on inequality
- With a focus on utility, inequality can increase
  - Even with strict fairness constraints
  - Even if group membership is known
  - Even if aggregate impact is larger



Approach	% Change in Impact Per-group							Aggregate % Impact	Disparity ( $\delta(z)$ )
	A	B	C	D	E	F	G		
No Intervention	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	$\pm 0.0$	1.429
IR	+1.76	+0.24	+0.42	+0.10	+0.16	+5.26	-1.35	+0.657	<b>1.386</b>
IR + 'no harm'	<b>+1.78</b>	+0.54	+0.74	+0.11	+1.02	<b>+5.56</b>	$\pm 0.0$	+0.848	1.394
DIP, $\tau = 0.567$	+1.20	+0.69	+1.46	<b>+0.63</b>	+1.61	+3.50	+0.43	+0.953	1.435
DIP, Unconstrained	+1.21	<b>+0.72</b>	<b>+1.48</b>	<b>+0.63</b>	<b>+1.64</b>	+3.51	<b>+0.47</b>	<b>+0.971</b>	1.435

# Counterfactuals for the Future

# Motivating toy example

## Treatment choice in a fixed sample

- Individualized treatment choice focused on **entire distribution of outcomes**
- **Allocating tutoring to students**
  - We want to allocate tutoring to students at a school in order to improve test performance
    - One time-step of past data on every student of interest
    - No confounding
    - We have a model of the data generating process
  - *Unobserved* external factors about the students (e.g., family income, encouragement from parents) explain at least some of the variation in the outcome across units



# Two approaches to the same problem

Which approach is better?

- **Approach 1:**
  - Use our model to identify which students to treat based on their covariate values only
- **Approach 2:**
  - Use our model to identify which students to treat based on their covariate values *and modeled exogenous variables (i.e., noise)*

# Two approaches to the same problem

Which approach is better?

- **Approach 1:** **Interventional**
  - Use our model to identify which students to treat based on their covariate values only
- **Approach 2:** **Counterfactual**
  - Use our model to identify which students to treat based on their covariate values *and modeled exogenous variables (i.e., noise)*



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- **Approach 2:** **Counterfactual**
  - Use our model to identify which students to treat based on their covariate values *and modeled exogenous variables (i.e., noise)*
- **Takeaway:** These two approaches can lead us to tutor a different set of students —> **two different policies**

# Motivating toy example

## Treatment choice in a fixed sample

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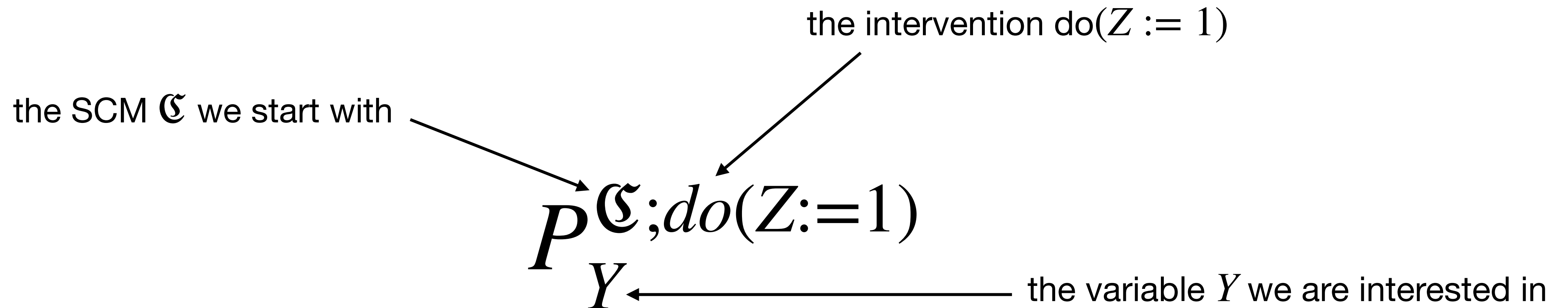
# Key question

What do we assume about family income and encouragement from parents year-to-year?

# Interventional distributions

## Notation

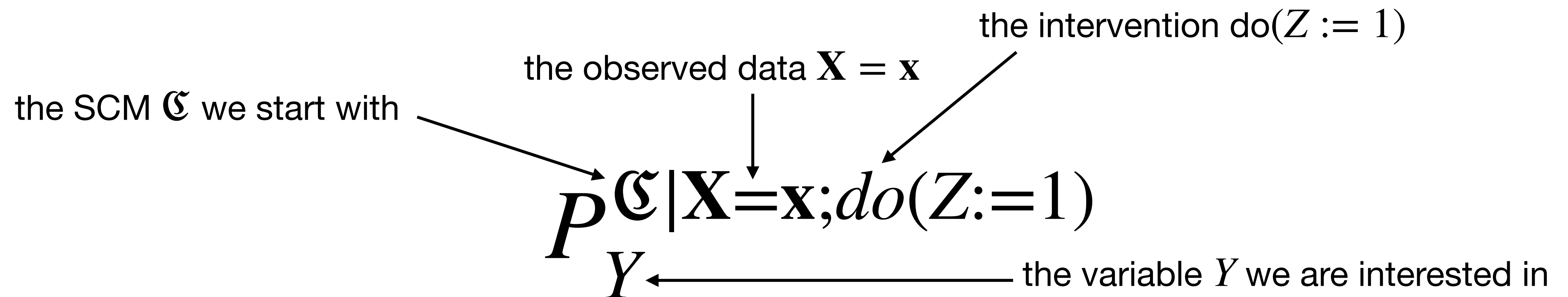
- Intuition:
  - “What will the distribution of test score  $Y$  be for a student described by SCM  $\mathcal{C}$  if they are enrolled in tutoring  $Z$ ?”



# Counterfactual distributions

## Notation

- Intuition:
  - “What would the distribution of test score  $Y$  **have been** for a student described by SCM  $\mathcal{C}$  if they **had been** enrolled in tutoring  $Z$ ?”



# Counterfactuals

## The retrospective view

- Counterfactuals are typically described as \*retrospective\*
  - We condition on \*observed circumstances\* before simulating an intervention
  - Use posterior  $P_{U|X=x}$  instead of prior  $P_U$  to obtain  $P_Y^{\mathcal{C}|X=x;do(\dots)}$
- **Our work:** When can (or should) counterfactuals be forward-looking?

# Why would we use past noise to make future decisions?

## Assumptions about what we haven't observed

- Common for data with multiple time steps
  - “There are unobserved variables that play an important role in our model”
  - Large literature: time-series cross sectional data, mixed effects models, latent variable models, etc.
  - Can use repeated observations for estimation
- **Our setting: data with one time-step**
  - Noise decomposition is no longer an estimation problem
    - No repeated observations
  - Accounting for unobserved variables is instead *based on assumptions*

# Forward-looking counterfactuals (FLCs)

## An alternate view

- The 'retrospective' view is connected to assumptions about the **structure** and **stability** of exogenous variables (noise)
  - Structure:
    - ▶ How does a unit look exogenously compared to other units?
  - Stability:
    - ▶ How does a unit look exogenously compared to itself over time?
- **Spoiler:** FLCs useful when units' exogenous factors are (1) sufficiently stable over time OR (2) sufficiently dissimilar to other units



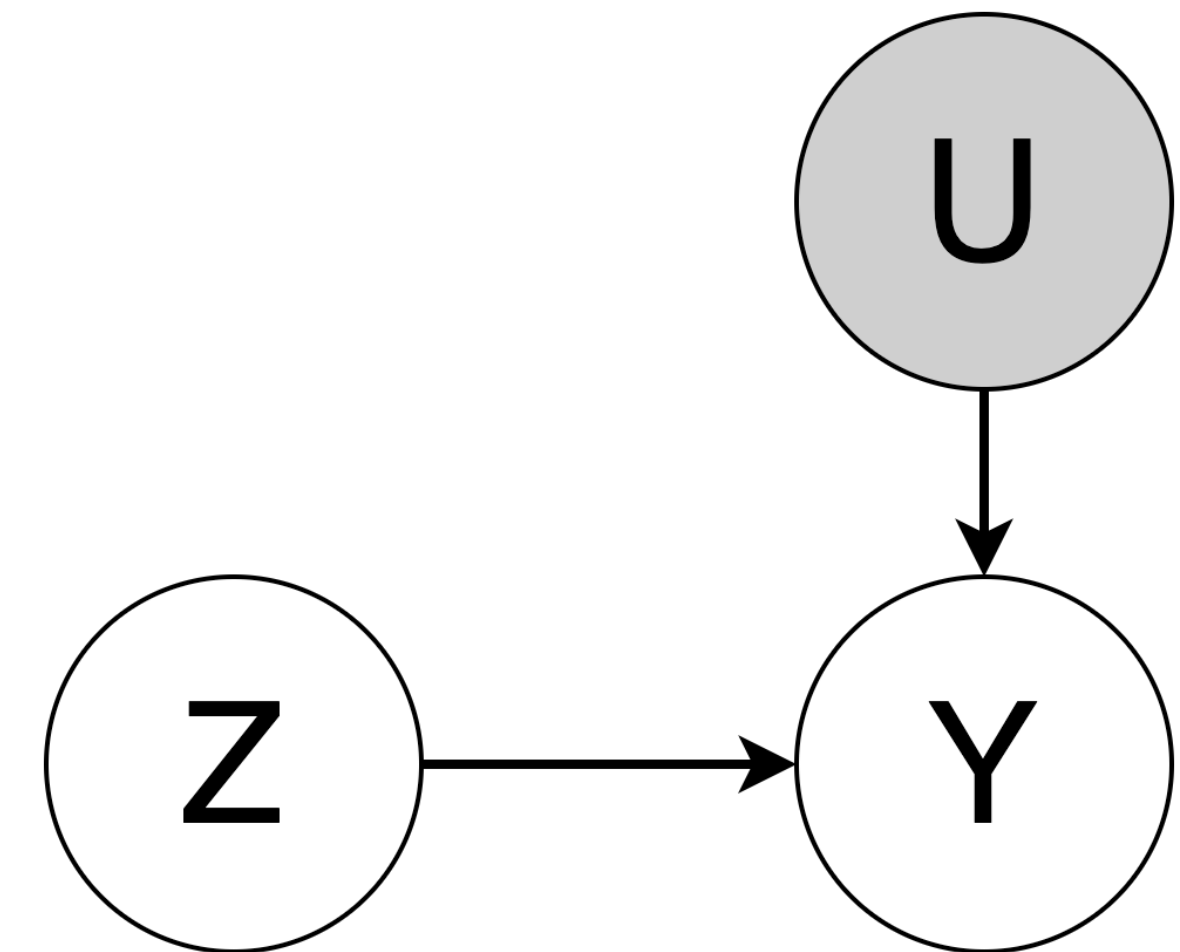
# Exploring FLCs empirically

## An illustrative parameterization

- Outcome  $Y$ , treatment  $Z$ , exogenous factors  $U$ , observed data  $\{Z_0^{(i)}, Y_0^{(i)}\}_{i=1}^n$
- Intervention on unit  $i$  will increase  $Z$  by amount  $\delta$
- **Goal:** recover distribution  $P_{Y_1}$  after intervention on those for whom  $Y_0 < 0$

$$(t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases} \quad (t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

Treatment choice



# Exploring FLCs empirically

## Model for exogenous noise terms

$$(t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$(t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

$$\mu_U^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2)$$
$$U_0^{(i)}, U_1^{(i)} \stackrel{iid}{\sim} \mathcal{N}(\mu_U^{(i)}, \sigma_U^2)$$

# Exploring FLCs empirically

## Model for exogenous noise terms

$$(t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$
$$(t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

We can now explore structure  
( $\sigma_\mu$ ) and stability ( $\sigma_U$ )

$$\mu_U^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2)$$
$$U_0^{(i)}, U_1^{(i)} \stackrel{iid}{\sim} \mathcal{N}(\mu_U^{(i)}, \sigma_U^2)$$

# Parameterizing exogenous structure and stability

## Connecting assumptions to parameters

Assumption	Model	Interpretation
(A1) Exogenous factors are constant over time.	$\sigma_U = 0$	Among the relevant variables we haven't measured, each unit looks exactly the same next year as it does this year.
(A2) Exogenous factors vary over time.	$\sigma_U > 0$	Among the relevant variables we haven't measured, each unit looks somewhat the same next year as it does this year. Similarities grow weaker with larger $\sigma_U$ values.
(A3) Exogenous factors exhibit unstructured variation.	$\sigma_\mu = 0$	Among the relevant variables we haven't measured, each unit looks the same as any other unit, apart from random variability with time.
(A4) Exogenous factors exhibit structured (unit-specific) variation.	$\sigma_\mu > 0$	Among the relevant variables we haven't measured, there are units that look unlike other units, in addition to random variability with time. Units look less like each other with larger $\sigma_\mu$ .

$$\mu_U^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2)$$
$$U_0^{(i)}, U_1^{(i)} \stackrel{iid}{\sim} \mathcal{N}(\mu_U^{(i)}, \sigma_U^2)$$

# Counterfactual vs. interventional distributions

What happens with a 'correct' model?

$$\mu_U^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2)$$

$$\text{Truth } (t = 0) : \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$\text{Truth } (t = 1) : \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ U_1^{(i)} \sim \mathcal{N}(\mu_U^{(i)}, \sigma_U^2) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{(i)} \end{cases}$$

$$\text{Model } (t = 0) = \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

$$\text{Interventional } (t = 1) = \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ U_1^{\prime(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_1^{(i)} = Z_1^{(i)} + U_1^{\prime(i)} \end{cases}$$

$$\text{Counterfactual } (t = 1) = \begin{cases} Z_1^{(i)} = Z_0^{(i)} + \delta \cdot w(i) \\ \tilde{U}_1^{(i)} = U_0^{(i)} \\ Y_1^{(i)} = Z_1^{(i)} + \tilde{U}_1^{(i)} \end{cases}$$

# Counterfactual vs. interventional distributions

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$P_{Y_1}$

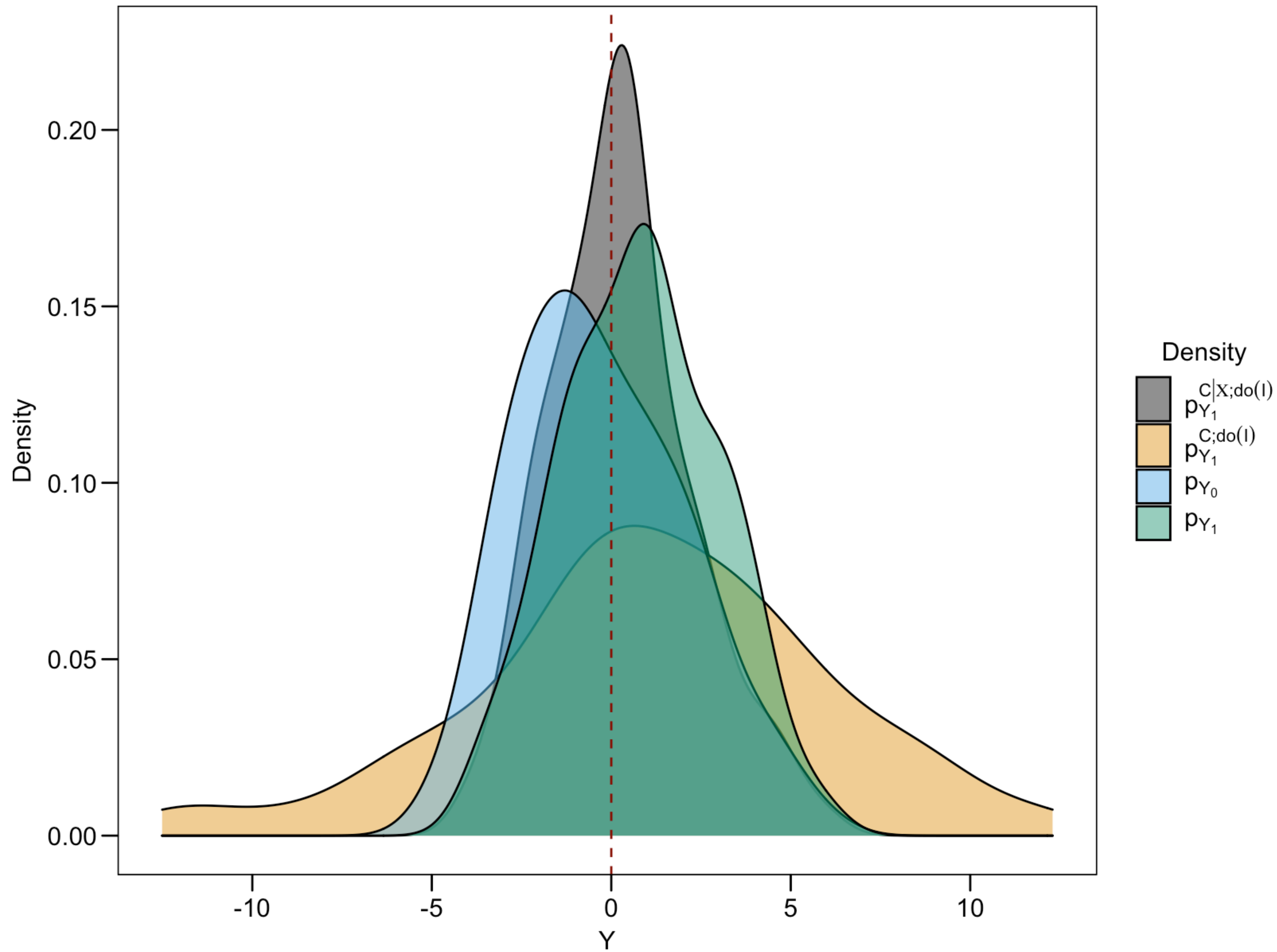
$$\text{Model } (t = 0) = \begin{cases} Z_0^{(i)} \sim \mathcal{N}(\mu_Z, \sigma_Z^2) \\ U_0^{(i)} \sim \mathcal{N}(0, \sigma_\mu^2 + \sigma_U^2) \\ Y_0^{(i)} = Z_0^{(i)} + U_0^{(i)} \end{cases}$$

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$P_{Y_1}^{\mathfrak{C}; do(\dots)}$

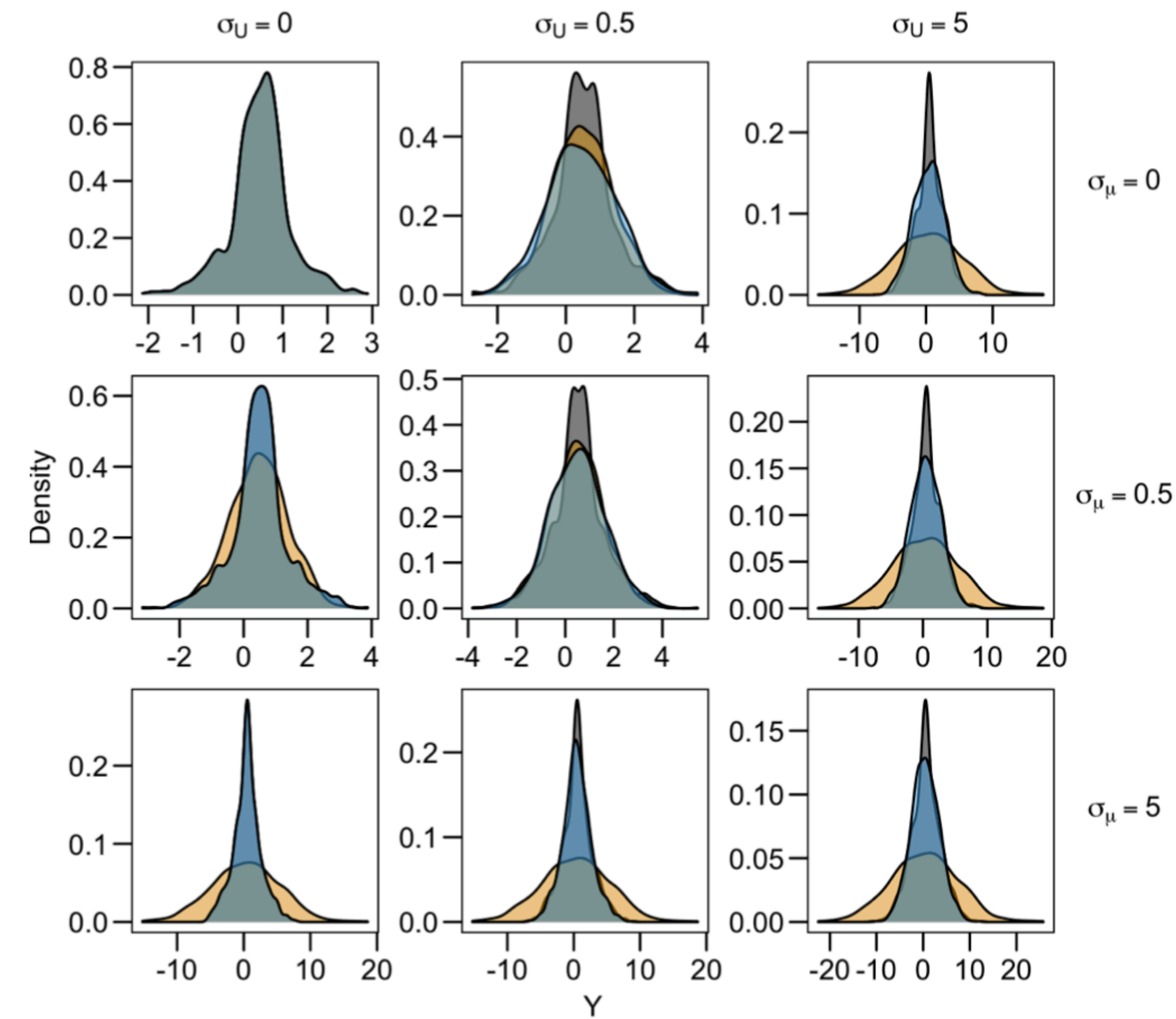
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$P_{Y_1}^{\mathfrak{C} | \mathbf{X}=\mathbf{x}; do(\dots)}$

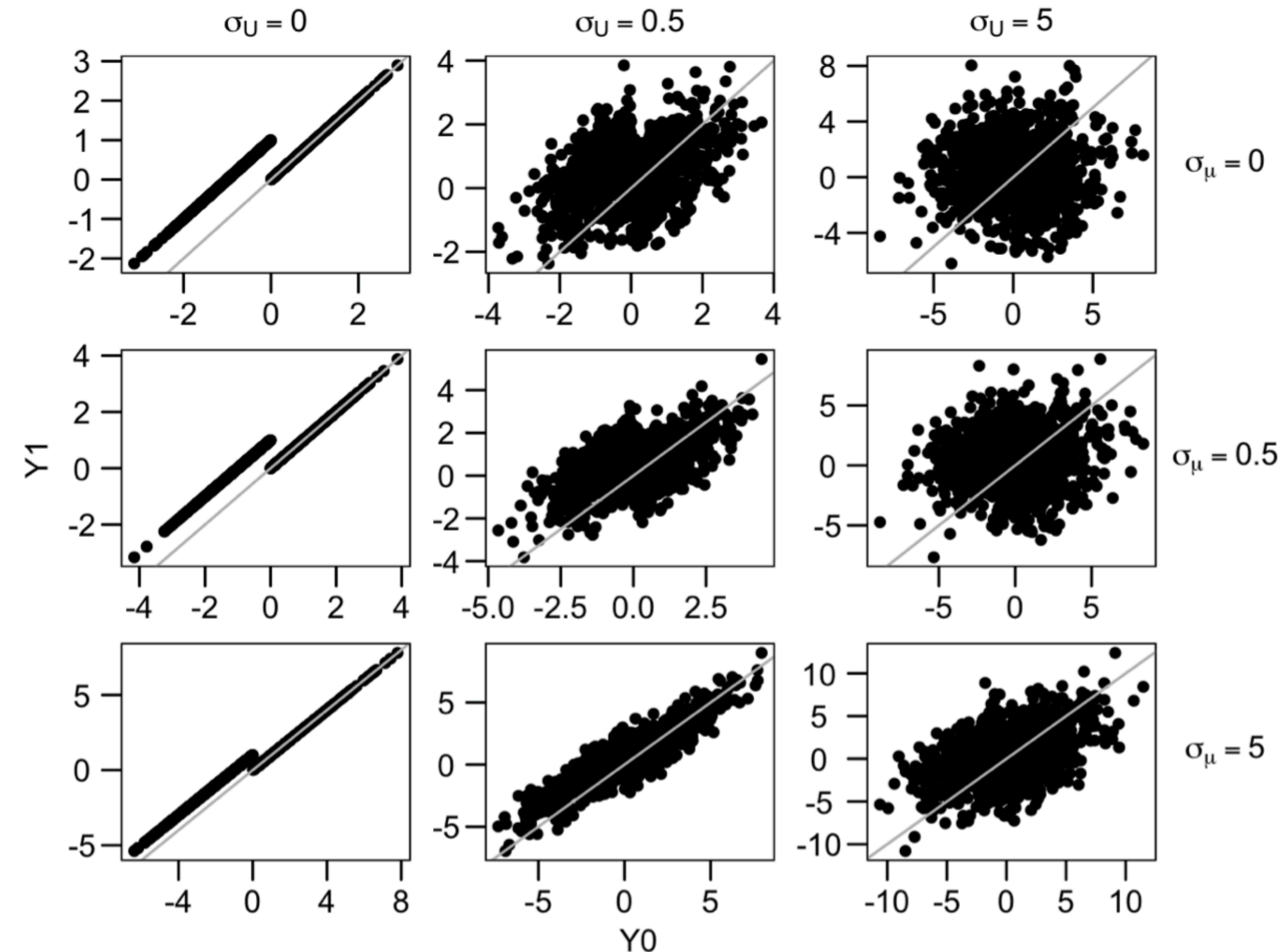


# Takeaways

Unit-specific structure OR stability over time  $\rightarrow$  FLCs



(a)



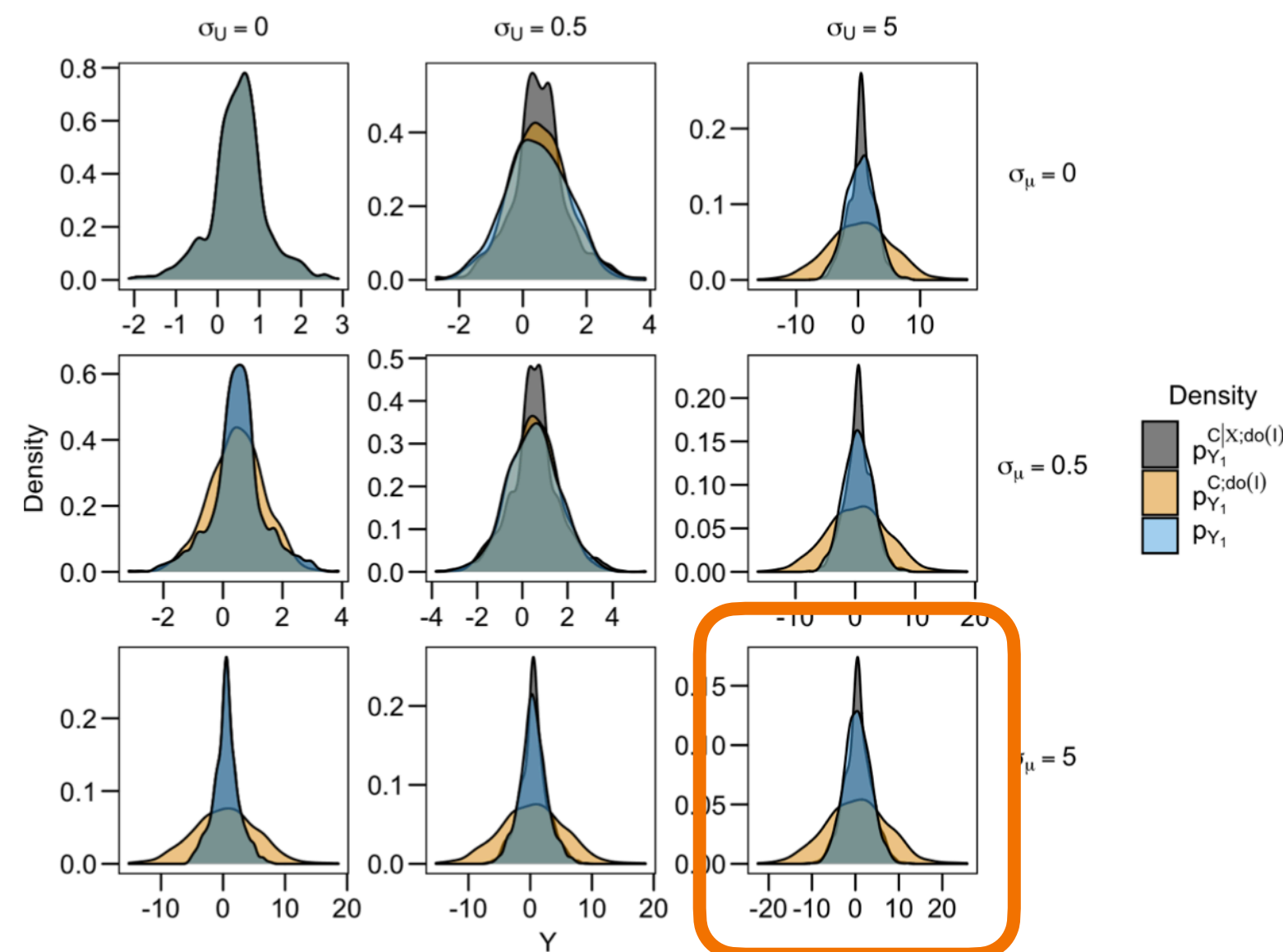
(b)



# Why do we care?

## Back to motivation

- We often can't measure every relevant variable
- We might not be able to collect lots of data over time
- Our assumptions can lead to **different policies** and **incorrect conclusions**



What if we want to decrease variance?

$\mathbb{V}[P_{Y_0}]$	$\mathbb{V}[P_{Y_1}]$	$\mathbb{V}[P_{Y_1}^{C X;do(I)}]$	$\mathbb{V}[P_{Y_1}^{C;do(I)}]$
12.2	9.36	9.61	51.1

# References 1

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**Thank you! Questions?**